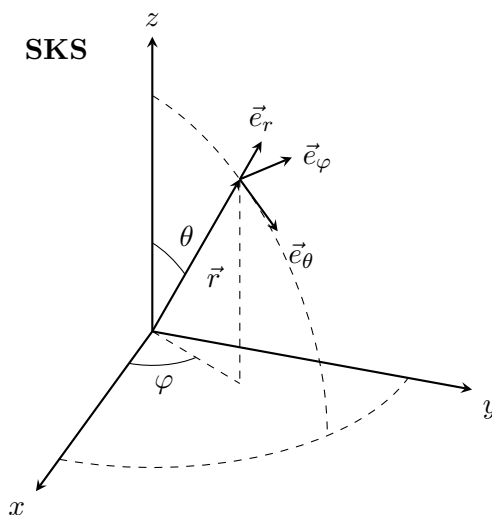
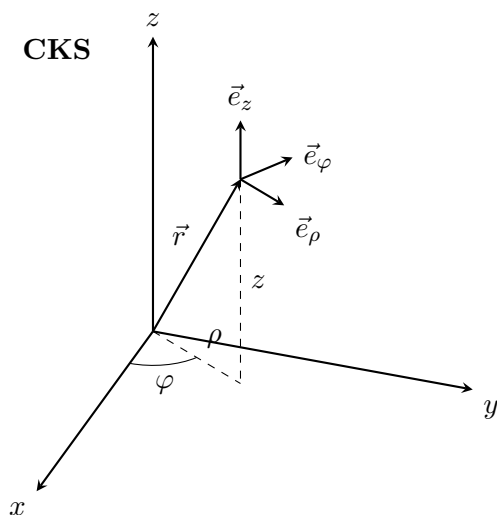


1 Koordinatni sistemi

KKK	$\vec{e}_x = \vec{i}$	$\vec{e}_y = \vec{j}$	$\vec{e}_z = \vec{k}$
\vec{r}	x	y	z
\vec{v}	\dot{x}	\dot{y}	\dot{z}
\vec{a}	\ddot{x}	\ddot{y}	\ddot{z}
CKS/PKS	\vec{e}_ρ	\vec{e}_φ	\vec{e}_z
\vec{r}	ρ	0	z
\vec{v}	$\dot{\rho}$	$\rho\dot{\varphi}$	\dot{z}
\vec{a}	$\ddot{\rho} - \rho\dot{\varphi}^2$	$\rho\ddot{\varphi} + 2\dot{\rho}\dot{\varphi}$	\ddot{z}
SKS	\vec{e}_r	\vec{e}_θ	\vec{e}_φ
\vec{r}	r	0	0
\vec{v}	\dot{r}	$r\dot{\theta}$	$r\dot{\varphi}\sin\theta$
\vec{a}	$\ddot{r} - r\dot{\theta}^2 - r\dot{\varphi}^2\sin^2\theta$	$r\ddot{\theta} + 2\dot{r}\dot{\theta} - r\dot{\varphi}^2\sin\theta\cos\theta$	$r\ddot{\varphi}\sin\theta + 2\dot{r}\dot{\varphi}\sin\theta + 2r\dot{\theta}\dot{\varphi}\cos\theta$
NKS	\vec{e}_t	\vec{e}_n	\vec{e}_b
\vec{r}	—	—	—
\vec{v}	\dot{s}	0	0
\vec{a}	\ddot{s}	$\kappa\dot{s}^2$	0



$$\begin{pmatrix} \vec{e}'_t \\ \vec{e}'_n \\ \vec{e}'_b \end{pmatrix} = \begin{pmatrix} 0 & \kappa & 0 \\ -\kappa & 0 & \tau \\ 0 & -\tau & 0 \end{pmatrix} \begin{pmatrix} \vec{e}_t \\ \vec{e}_n \\ \vec{e}_b \end{pmatrix}$$

$$\vec{S} = \frac{1}{2} \vec{r} \times \vec{v}$$

$$S = \frac{1}{2} \rho^2 \dot{\varphi} \text{ (PKS)}$$

$$ds = \sqrt{dx^2 + dy^2 + dz^2}$$

$$\vec{e}_t = \vec{r}'; \quad R_{pr} = \frac{1}{\kappa}$$

2 Kinematika togega telesa

$$\vec{v} = \vec{\omega} \times \vec{r}$$

$$\vec{v}_2 = \vec{v}_1 + \vec{\omega} \times \vec{\rho}_{12}$$

$$\vec{a}_2 = \vec{a}_1 + \vec{\alpha} \times \vec{\rho}_{12} - \omega^2 \vec{\rho}_{12}$$

$$\lambda = \frac{\pi}{2}, \quad \rho = \frac{v}{\omega} \text{ (pol hitrosti)}$$

$$\sin \lambda = \frac{\alpha \rho}{a}, \quad \cos \lambda = -\frac{\omega^2 \rho}{a} \text{ (pol pospeška)}$$

$$\tan \lambda = -\frac{\alpha}{\omega^2}, \quad \rho = \frac{a}{\sqrt{\alpha^2 + \omega^4}}$$

3 Dinamika togega telesa

$$I_{ij} = \sum_k m_k (r_k^2 \delta_{ij} - r_{ik} r_{jk})$$

$$\vec{L} = \vec{I} \vec{\omega}, \quad E_{\text{kin}} = \frac{1}{2} \vec{\omega} \cdot \vec{L}$$

$$\vec{M} = \frac{d\vec{L}}{dt} = \left(\frac{d\vec{L}}{dt} \right)_{\text{tel}} + \vec{\omega} \times \vec{L}$$

$$I_1 \dot{\omega}_1 + (I_3 - I_2) \omega_2 \omega_3 = M_1$$

$$I_2 \dot{\omega}_2 + (I_1 - I_3) \omega_3 \omega_1 = M_2$$

$$I_3 \dot{\omega}_3 + (I_2 - I_1) \omega_1 \omega_2 = M_3$$

4 Langrangeova enačba

$$L = T - V$$
$$\frac{d}{dt} \left(\frac{\partial L}{\partial \dot{q}_i} \right) - \frac{\partial L}{\partial q_i} = 0$$

$$L = T - V$$
$$\frac{d}{dt} \left(\frac{\partial L}{\partial \dot{q}_i} \right) - \frac{\partial L}{\partial q_i} = \sum_j a_{ji} \lambda_j \text{ (} i\text{-ta koordinata)}$$
$$\sum_i a_{ji} \dot{q}_i = 0 \text{ (} j\text{-ti pogoj)}$$